



University of  
South Australia

## Position Paper:

# On Extending the Sweep-Line for Language Equivalence Checking

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Kindly presented by Lars Michael Kristensen

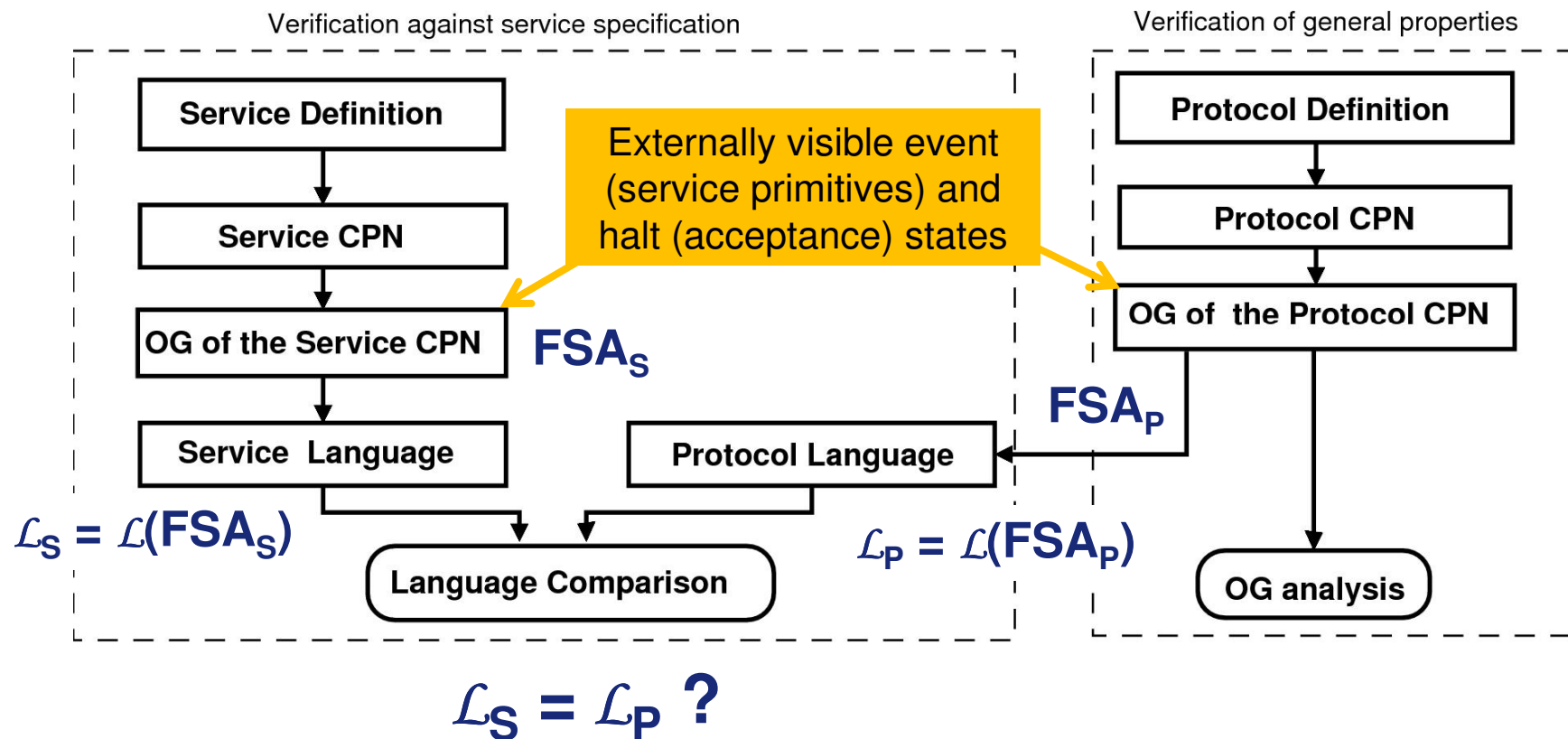
.. who made small and non-substantial modifications to  
this slide set that only he can be held responsible for...



# Background and Motivation

## Protocol Verification Methodology:

1. Verification of general properties: absence of deadlocks, livelocks...
2. Verification against its **service specification**.





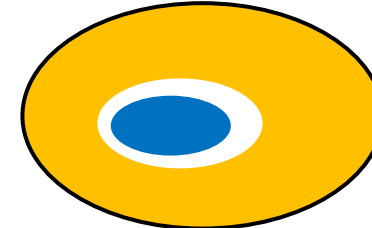
# Background and Motivation

- **Question** - language equivalence checking with **sweep-line exploration**?
  - Service language:  $\mathcal{L}_S$  Protocol language:  $\mathcal{L}_P$  Equivalence:  $\mathcal{L}_S = \mathcal{L}_P$
  - $\mathcal{L}_P \subseteq \mathcal{L}_S$ : All behaviour of the protocol is allowed by the service specification.
  - $\mathcal{L}_S \subseteq \mathcal{L}_P$ : The protocol implements (at least) all of its service.
- **Previous work** – protocol language inclusion checking, i.e.,  $\mathcal{L}_P \subseteq \mathcal{L}_S$ :
  - All user-observable behaviour exhibited by the protocol is acceptable.
  - Acceptable in some circumstances, provided the protocol implements an **acceptable subset** of the service (determining this is a problem in its own right).
- **This position paper** - extension to language equivalence checking:
  - Can we simply check language inclusion and then the reverse, e.g. check  $\mathcal{L}_P \subseteq \mathcal{L}_S$  and  $\mathcal{L}_S \subseteq \mathcal{L}_P$  which would imply that  $\mathcal{L}_S = \mathcal{L}_P$ .
  - **No!** the OG of the protocol is prohibitively large, hence the use of sweep-line.
  - Requires extension of the sweep-line method with **on-the-fly determinisation**.



# Language Inclusion Checking

- **Question** - language equivalence checking with **sweep-line exploration**?
  - Service language:  $\mathcal{L}_S$  Protocol language:  $\mathcal{L}_P$  Equivalence:  $\mathcal{L}_S = \mathcal{L}_P$
  - $\mathcal{L}_P \subseteq \mathcal{L}_S$ : All behaviour of the protocol is allowed by the service specification.
  - $\mathcal{L}_S \subseteq \mathcal{L}_P$ : The protocol implements (at least) all of its service.
  - **Earlier work** – protocol language inclusion checking, i.e.,  $\mathcal{L}_P \subseteq \mathcal{L}_S$  :
    - All user-observable behaviour exhibited by the protocol is acceptable.
    - This holds if  $\mathcal{L}(\overline{\text{FSA}_S}) \cap \mathcal{L}(\text{FSA}_P) = \mathcal{L}(\overline{\text{FSA}_S} \parallel \text{FSA}_P)$  is empty:

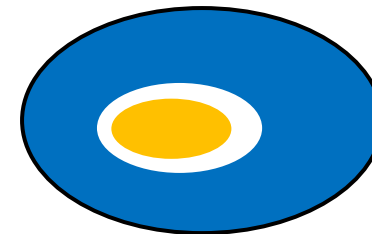


- $\text{FSA}_S$  must be **deterministic** in order to obtain its complement.
- Determinisation not usually a problem for  $\text{FSA}_S$ :
  - It is small enough to be known a priori, hence can be made deterministic and its complement found prior to exploring the protocol OG.
  - Both mapping from the OG to the FSA and the parallel composition of service and protocol FSAs can be performed on-the-fly with the sweep-line method.



# Language Equivalence Checking

- **This position paper** - extension to language equivalence checking:
  - Can we simply check language inclusion and then the reverse, e.g. check  $\mathcal{L}_p \subseteq \mathcal{L}_s$  and  $\mathcal{L}_s \subseteq \mathcal{L}_p$  which would imply that  $\mathcal{L}_s = \mathcal{L}_p$  ?
  - **No!** the OG of the protocol is prohibitively large (hence the use of sweep-line).
- Checking  $\mathcal{L}_s \subseteq \mathcal{L}_p$  - the protocol implements (at least) all of the service:
  - This holds if  $\mathcal{L}(\text{FSA}_s) \cap \mathcal{L}(\overline{\text{FSA}_p}) = \mathcal{L}(\text{FSA}_s \parallel \overline{\text{FSA}_p})$  is empty, :

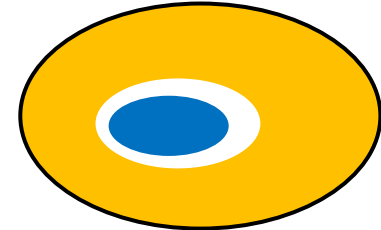


- This time  $\text{FSA}_p$  must be deterministic - but  $\text{FSA}_p$  (protocol OG) is large due to state explosion.
- Determinisation, complement, and parallel composition must be done on-the-fly during sweep-line exploration.
- Requires extension of the sweep-line method with **on-the-fly determinisation**.

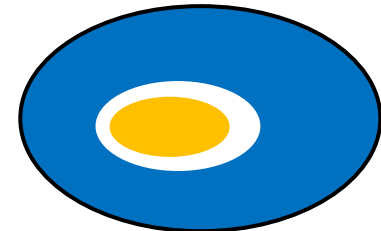


# Language Equivalence Checking

- Checking  $\mathcal{L}_P \subseteq \mathcal{L}_S$  - protocol has not illegal behaviours:
  - This holds if  $\mathcal{L}(\overline{\text{FSA}_S} \parallel \text{FSA}_P)$  is empty.
  - $\text{FSA}_S$  must be **deterministic** in order to obtain its complement.
  - Determinisation not usually a problem for  $\text{FSA}_S$ :
    - It is small enough to be known a priori, hence can be made deterministic and its complement found prior to exploring the protocol OG.
    - Both mapping from the OG to the FSA and the parallel composition of service and protocol FSAs can be performed on-the-fly with the sweep-line method.



- Checking  $\mathcal{L}_S \subseteq \mathcal{L}_P$  - the protocol implements (at least) all of the service:
  - This holds if  $\mathcal{L}(\text{FSA}_S) \cap \mathcal{L}(\overline{\text{FSA}_P}) = \mathcal{L}(\text{FSA}_S \parallel \overline{\text{FSA}_P})$  is empty,
  - but this time  $\text{FSA}_P$  must be deterministic.



- The  $\text{FSA}_P$  (protocol OG) is large due to state explosion (which is why we want use the sweep-line method)
- Determinisation, complement, and parallel composition must be done on-the-fly during sweep-line exploration.



# Language Equivalence Checking

- **Exactly what must we do on-the-fly?**
  1. **Map from the Protocol OG to  $FSA_p$** 
    1. Arc labels map to service primitives or epsilon
    2. Recognise halt (acceptance) states
  2. **Determinise  $FSA_p$  to produce  $DFSA_p$**
  3. **Produce the complement of  $DFSA_p$** 
    1. Introduce a “trap” state
    2. “complete” the FSA  
(all states accept all symbols, leading to the trap state when not previously defined)
    3. Invert halt states
- **Mapping from the OG to the FSA (1) and producing the complement of  $DFSA_p$  (3) can be done on a state-by-state and arc-by-arc basis.**
- **The non-trivial part is on-the-fly determinisation in presence of states being deleted from memory by the sweep-line method.**



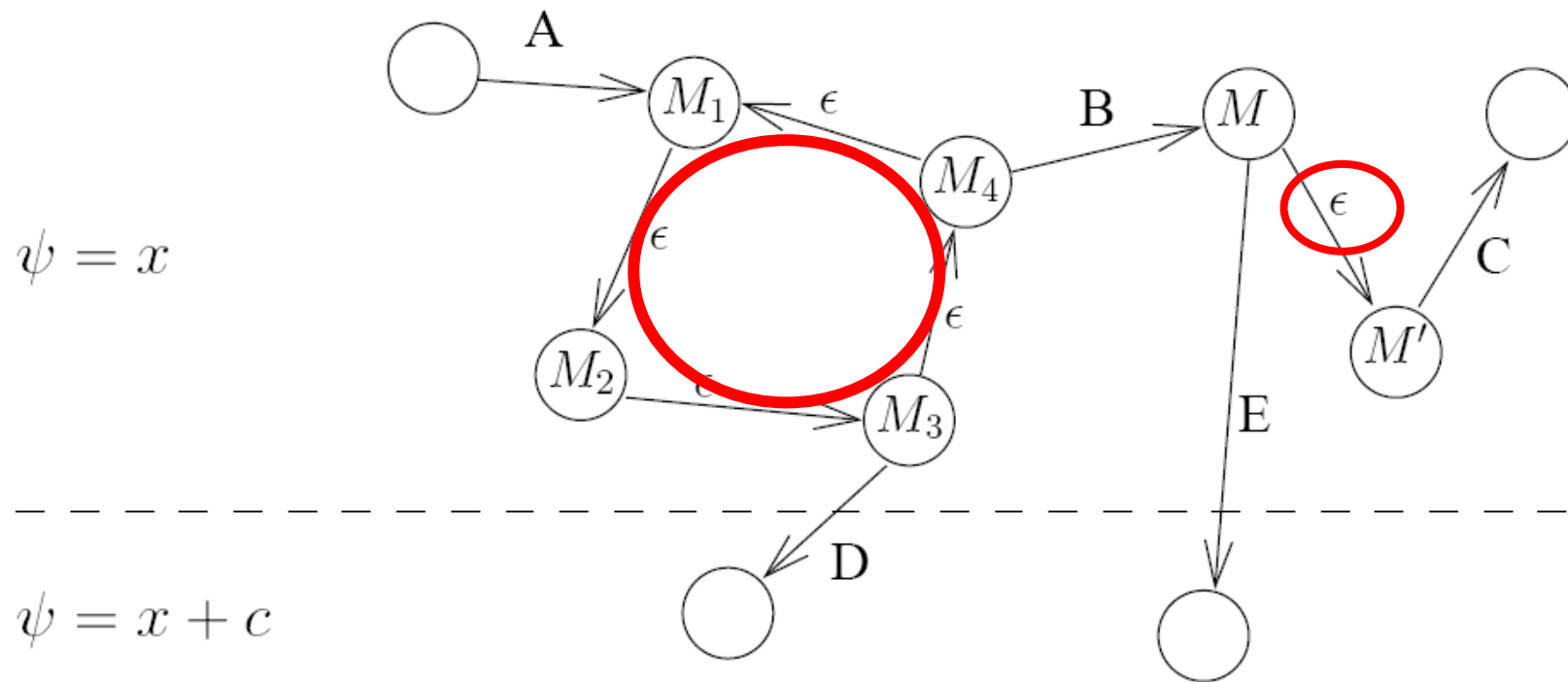
# Language Equivalence Checking

- **On-the-fly determinisation with the sweep-line method lends itself to a state-by-state (level-by-level) approach:**
  - We adopt the techniques of e.g. Barrett and Couch [1]:
    - Remove empty (epsilon) cycles
    - Remove remaining empty (epsilon) moves
    - Remove remaining non-determinism
  - **Challenge:** empty cycles and empty moves may cross progress-level boundaries.
  - When it is safe for states to be deleted from memory?
  - Introduce **transient states** in addition to **persistent states**:
    - **Persistent states:** cannot be deleted (destinations of regress edges).
    - **Transient states:** must be retained in memory for now, for the purposes of determinisation, but can be deleted at some point in the future.





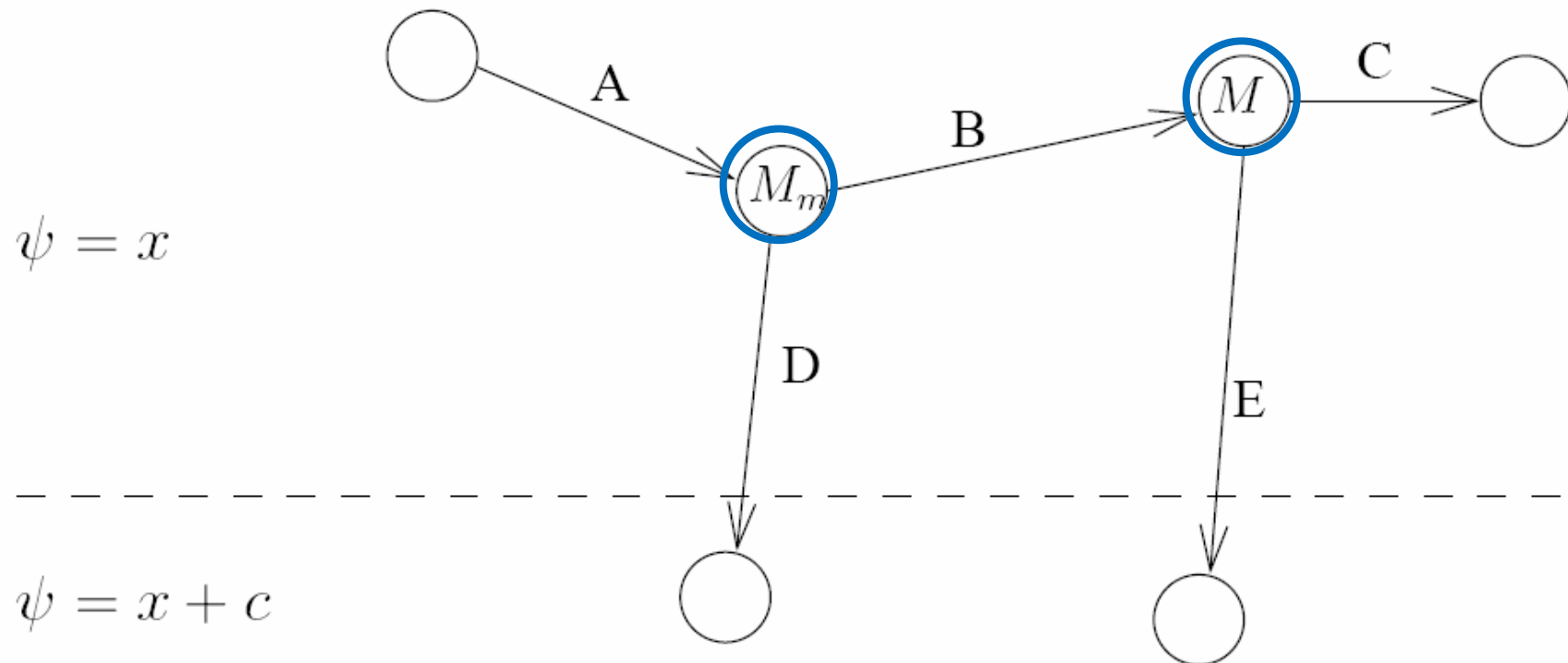
# Example: Some Simple Situations



Progress  
value



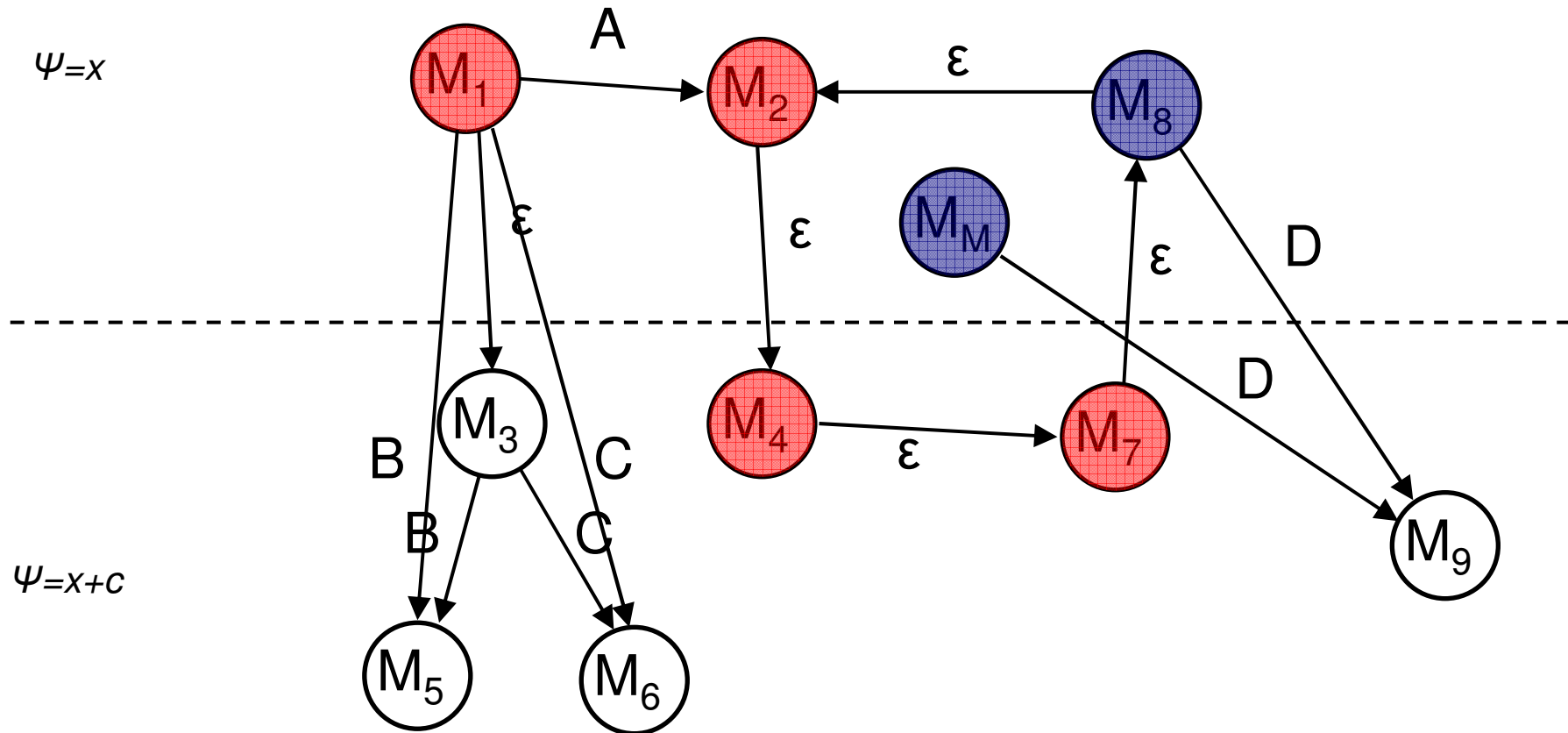
# Example: Some Simple Situations



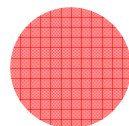
Progress  
value

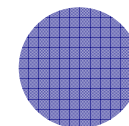


# Example: Some Complex Situations



Progress  
value

 = transient

 = persistent



# Conclusions and Future Work

- **This extension of the sweep-line method as presented in this position paper is at an early stage of development.**
  - We have adopted the two-step approach as advocated by e.g. [1].
  - Much work remains to bring this work to fruition.
- **The key is knowing when states must be temporarily retained for the purposes of determinisation, after which they can be deleted.**
  - Not all examples are captured in the paper.
- **It remains to:**
  - Formalise the approach and verify its termination properties (currently a conjecture).
  - Develop a modified sweep-line exploration algorithm that takes into account on-the-fly determinisation.
  - Evaluate its effectiveness on a substantial case study.
- **Determinisation can be interleaved with the complementation and parallel composition activities**
  - It remains to be seen whether full interleaving of these activities or “batch” processing is more efficient/effective.



# Conclusions and Future Work

- We have adopted the two-step approach as advocated by e.g. [1].
- Determinisation via the power set/subset construction technique (e.g. [15]) with lazy subset evaluation is another approach that may be investigated
  - States of the deterministic FSA are power sets of the set of global states.
  - “Lazy” evaluation: calculate subsets (epsilon-closures) only as they are required.
  - Intuitively, exploring all successors reachable via epsilon moves is less suited to Sweep-line analysis, as this may frequently violate the Sweep-line’s “least-progress-first” exploration policy.
  - It should be possible to defer the calculation of epsilon-closures, however this results in an algorithm that looks remarkably similar to the one already adopted.
- If our goal is simply to detect a violation of language equivalence, it may be possible to take a more direct approach in some cases:
  - The parallel composition of  $FSA_S$  and  $FSA_P$  (not its complement) can be built on-the-fly and the symbols accepted by each state compared with the corresponding states in  $FSA_S$  and  $FSA_P$ .
  - If they don’t match, we have a violation of language equivalence.
  - On-the-fly complementation is no longer required, however, the hard work of determinisation still is.



# A Final Acknowledgement

**I would like to sincerely thank Lars Kristensen for the discussions we held on this topic many years ago, and especially for agreeing to present this on my behalf.**

**Thankyou Lars!**



# Questions?

