



University of  
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Position Paper  
Relaxed Timed Coloured Petri Nets  
A Motivational Case Study

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## Scheduling applications:

- We have used both Timed and Untimed CPNs for a number of task scheduling projects involving time.
  - Timed CPNs exhibit an *eagerness-to-execute* semantics which may exclude the discovery of *optimal schedules*.
  - Untimed CPNs do not exhibit this property, hence allow all possible *sequences* of events without regard to timing, including sequences that correspond to optimal schedules.
  - When timing is imposed on the untimed sequences, we discover the globally optimal schedules, but also *infeasible* schedules – schedules that are not realisable.
- Ideally, we want a time semantics that captures all feasible schedules (including optimal) and no infeasible schedules.
  - A time semantics relaxing the eagerness-to-execute property.



Consider a set of tasks that are executed to reach a ***goal state***

## Task Characteristics:

- A duration
- Require preconditions and produce effects that become preconditions of future tasks.
- May require resources.

# Three Task Example

Consider three tasks:

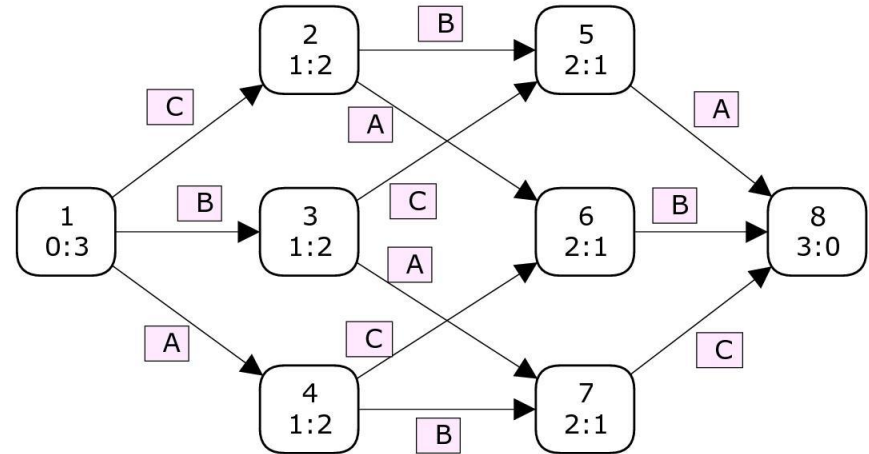
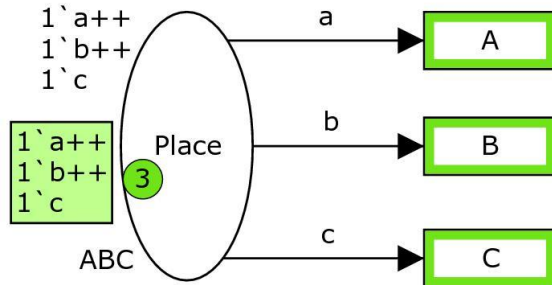
Task	Precondition	Effect	Required Resources	Duration
T1	C1	C2	R1	5
T2	C1	C2	R2	50
T3	C2	C3	R2	10

**Initial state:** C1 holds. **Goal state:** C3 holds.

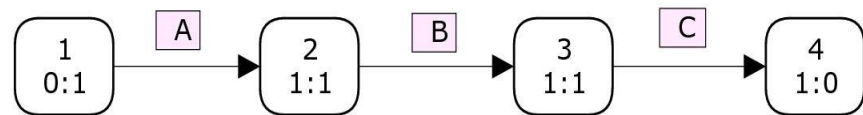
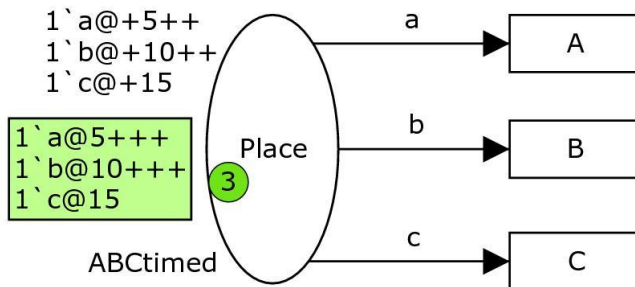
- Both T1 and T2 can and do start at time 0
- T3 requires R2, hence cannot start until after T2 terminates and releases R2, at time 50
- **Goal state reached** when T3 terminates, at time **60**

**But** if T2 was delayed (or not executed at all), T3 could start as soon as T1 terminates. The **goal** would be **reached** at time **15**

## Untimed CPN and its RG:



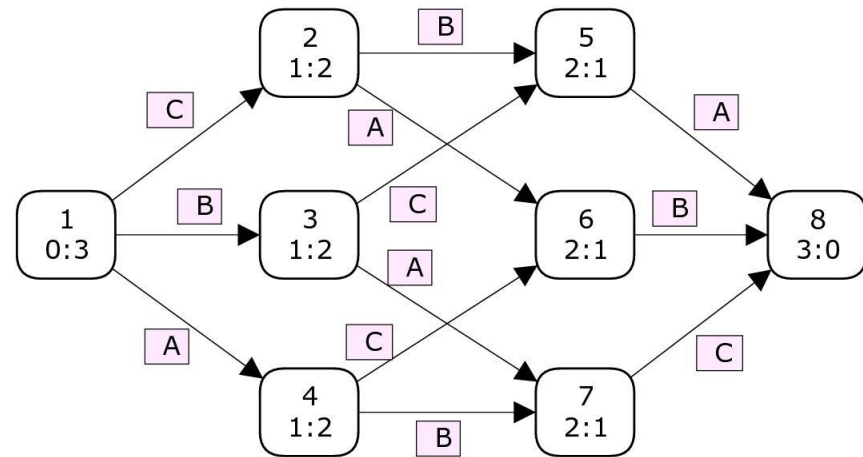
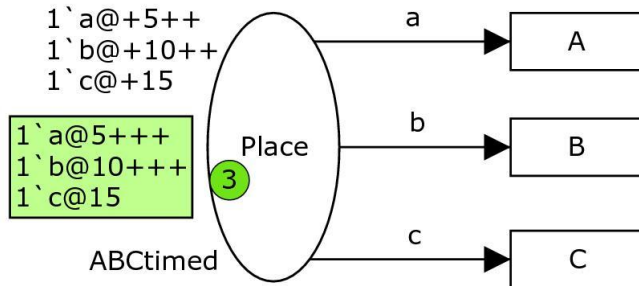
## Timed CPN and its RG:



# Relaxed Time Semantics

**Basic idea:** remove the restriction that the next binding element to occur must have the minimum time of all enabled binding elements.

**Relaxed Timed CPN and its RG:**



# Relaxed Time Semantics

## **Current Timed CPN enabling rule (see Def 11.6 in new CPN book):**

**A step,  $Y$ , is enabled at time  $t'$  in a timed marking,  $(M, t^*)$  (where  $t^*$  is the value of the global clock in marking  $M$ ), if and only if:**

1. The binding  $b$  of each binding element  $(t, b)$  in step  $Y$  satisfies the guard of  $t$ ;
2. Sufficient tokens exist in all untimed input places to satisfy the multiset sum of evaluated untimed input arc expressions for all binding elements in step  $Y$ ;
3. Sufficient and appropriately timed tokens exist in all timed input places to satisfy the multiset sum of timed input arc expressions evaluated for  $b$  at time  $t'$  for all binding elements in step  $Y$ ;
4. The current global clock,  $t^*$ , is less than or equal to  $t'$ ; and
5.  $t'$  is the smallest time value for which there exists a step satisfying conditions 1 to 4.

## **Modified enabling rule for Relaxed Timed CPNs:**

5.  $t'$  is the smallest time value that satisfies conditions 1 to 4 for step  $Y$ .



## Idea:

**A subset of transitions may be required to occur at the earliest opportunity.**

- E.g. transitions that represent termination of tasks that have a fixed duration should not be delayed
- Removes infeasible schedules

**Allows the generation of a whole spectrum of RGs:**

- From the RG of the existing Timed CPNs (no transitions can be delayed)
- To the RG obtained when all transitions can be delayed (fully relaxed Timed CPNs)



# Conclusions

- **Propose a relaxation of the semantics of Timed CPNs**
  - some or all of the transitions can be excluded from the *eagerness-to-execute* property.
- **Conjecture: the proposal preserves the same properties as the existing semantics of Timed CPNs with respect to preservation of markings and occurrence sequences of the corresponding untimed CPN.**
  - hence the new time semantics has the potential to be applied to the analysis of any system currently modelled by Timed CPNs.
- ***In Particular* the new semantics allows**
  - **all** schedules to be captured by the RG, and hence the determination of **optimal schedules**.
  - **infeasible schedules** to be removed



# Future Work

- **Establish a firm theoretical foundation**
- **Prove the preservation of markings and occurrence sequences**
- **Provide support in CPN Tools**
- **Investigate the use of this modified time semantics in a case study of significance, such as our operational planning work.**