## madalgo - -**CENTER FOR MASSIVE DATA ALGORITHMICS**

# Approximating the Diameter of Large Graphs





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- Compute a spanning tree of the input graph
- Build an Euler tour around it and chop it into O(n/k) clusters of length k
- Eliminate duplicates by keeping only the first occurrence
- Form a new (smaller) graph G'
  - Each node represents a non-empty cluster in the original graph Edge {C(u), C(v)} exists in G' if the edge {u, v} exists in G
- Run Breadth-First Search on G' starting from an arbitrary node

[1] Ulrich Meyer. On Trade-Offs in External-Memory Diameter-Approximation. SWAT 2008.

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### **Breadth-First Search Tree**

- Height of a Breadth-First Search tree gives a 2-approximation to the diameter of the graph
- Computing Breadth-First Search requires days for large graphs with billions of edges, even with the most efficient external memory algorithms
- Need to approximate the diameter even faster than the Breadth-First Search traversal of the graph
- We perform an empirical study to compare the running time and approximation quality of different algorithms

### Euler Tour Based Algorithm

### References