Analyzing JavaScript Web Applications

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JavaScript: the lingua franca of Web 2.0

JavaScript is a *dynamic language*

- Object-based
- Prototype-based inheritance
- First-class functions, closures
- Runtime types
- …

NO STATIC TYPE CHECKING

How JavaScript was designed

"I hacked the JS prototype
in ~1 week. And it showed!
Mistakes were frozen early."

– Brendan Eich, inventor of JavaScript

JavaScript

Static type analysis to the rescue!

```
var x = {
    a: 42,
    b: function() {return a;}
}
print(x.b())
```

an *abstract state* for each program point,
analyze it further to detect likely programming errors

<u>Potential</u> programming errors

1. invoking a non-function value (e.g. undefined) as a function
2. reading an absent variable
3. accessing a property of `null` or `undefined`
4. reading an absent property of an object
5. writing to variables or object properties that are never read
6. calling a function object both as a function and as a constructor, or passing function parameters with varying types
7. calling a built-in function with an invalid number of parameters, or with a parameter of an unexpected type

etc…

Flow of control and data can be subtle

```
function Person(n) {
    this.setName(n);
    Person.prototype.count++;
}
Person.prototype.count = 0;
Person.prototype.setName = function(n) { this.name = n; }
function Student(n,s) {
    this.b = Person;
    this.b(n);
    delete this.b;
    this.studentid = s.toString();
}
Student.prototype = new Person;

var t = 100026.0;
var x = new Student("Joe Average", t++);
var y = new Student("John Doe", t);
y.setName("John Q. Doe");
```

declares a "class" named Person

declares a "static field" named count

declares a shared method named setName

declares a "sub-class" named Student

creates two Student objects…

does y have a `setName` method at this program point?

An abstract state
(as produced by our analysis)

General and widely used approaches

- *The monotone framework*
  [Kam & Ullman '77]

- *The functional approach*
  [Sharir & Pnueli '81]

- *IFDS*
  [Reps, Horwitz, and Sagiv '95]

- ...

Our approach

- Abstract interpretation using the monotone framework

- The recipe:
  1. construct a **control flow graph** for the program to be analyzed

  2. define an appropriate **dataflow lattice** (abstraction of data)

  3. define **transfer functions** (abstraction of operations)

Control flow graphs

- declare-variable[x]

- read-variable[x,v]

- write-variable[v,x]

- constant[c,v]

- read-property[$v_{obj},v_{property},v_{result}$]

- write-property[$v_{obj},v_{property},v_{value}$]

- delete-property[$v_{obj},v_{property},v_{result}$]

- if[v]

- entry[$f,x_1,...,x_n$], exit, exit-exc

- call[$w,v_0,...,v_n$], construct[$w,v_0,...,v_n$], after-call[v]

- return[v]

- throw[v], catch[x]

- <op>[v_1,v_2], <op>[v_1,v_2,v_3]

- ...

- Convenient representation of JavaScript programs

- *Nodes* describe primitive instructions, *edges* describe control-flow

- Each *x* is a program variable

- Each *v* is a temporary variable (i.e. a register)

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Analysis lattice

the analysis lattice

abstract states

abstract objects

abstract values

Abstract values

object labels
(allocation sites)

$$\text{Value} = \text{Undef} \times \text{Null} \times \text{Bool} \times \text{Num} \times \text{String} \times \mathcal{P}(L)$$

$$\text{Undef} = \begin{array}{c} \text{undef} \\ | \\ \bot \end{array} \qquad \text{Null} = \begin{array}{c} \text{null} \\ | \\ \bot \end{array} \qquad \text{Bool} = \begin{array}{c} \text{bool} \\ \diagup \diagdown \\ \text{true} \quad \text{false} \\ \diagdown \diagup \\ \bot \end{array}$$

$$\text{Num} = \begin{array}{c} \text{Num} \\ \text{INF} \quad \text{UInt} \quad \text{NotUInt} \\ -\text{Inf} \ +\text{Inf} \ \text{NaN} \ 0 \ \cdots \ 4294967295 \quad \cdots -42 \ -1.87 \ 1.2 \ \cdots \\ \bot \end{array}$$

$$\text{String} = \begin{array}{c} \text{string} \\ \text{UIntString} \quad \text{NotUIntString} \\ \text{"0"}\cdots\text{"4294967295"} \ \text{"foo"}\cdots\text{"bar"} \\ \bot \end{array}$$

Example: $(\bot, \text{null}, \text{true}, 42.0, \bot, \{\ell_7, \ell_9\})$

Abstract objects

property names including [[Prototype]]

$$Obj = (\mathcal{P} \hookrightarrow Value \times Absent \times Attributes \times Modified) \times \mathcal{P}(ScopeChain)$$

(explained later)

describes the

[[Scope]] property

$$Absent = \begin{array}{c} absent \\ | \\ \bot \end{array} \qquad Modified = \begin{array}{c} modified \\ | \\ \bot \end{array}$$

$$Attributes = ReadOnly \times DontDelete \times DontEnum$$

$$ReadOnly = \begin{array}{c} \top \\ RO \quad notRO \\ \bot \end{array} \qquad DontDelete = \begin{array}{c} \top \\ DD \quad notDD \\ \bot \end{array} \qquad DontEnum = \begin{array}{c} \top \\ DE \quad notDE \\ \bot \end{array}$$

Abstract states

heap

$$\text{State} = (L \hookrightarrow \text{Obj}) \times \text{Stack} \times \mathcal{P}(L) \times \mathcal{P}(L)$$

(explained later)

temporary variables

the current
activation record

stack-reachable
objects

$$\text{Stack} = (T \rightarrow \text{Value}) \times \mathcal{P}(\text{ExecutionContext}) \times \mathcal{P}(L)$$
$$\text{ExecutionContext} = \text{ScopeChain} \times L \times L$$
$$\text{ScopeChain} = L^*$$

the `this` object

for resolving variables

the variable object,
for variable declarations

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The analysis lattice

$$AnalysisLattice = C \times N \rightarrow State$$

contexts

(for context sensitivity)

the flow graph nodes

Transfer functions

Example: **read-property**$[v_{obj}, v_{property}, v_{result}]$

1. Coerce v_{obj} to objects

2. Coerce $v_{property}$ to strings

3. Descend the object prototype chains
   (using the [[Prototype]] property)
   to find the relevant properties

4. Join the property values

5. Assign the result to v_{result}

Weak vs. strong updates

- For a **write-property**$[v_{obj}, v_{property}, v_{value}]$ node, v_{obj} refers to one or more abstract objects (identified by their allocation sites)

- Each abstract object generally describes *multiple* concrete objects

- So **write-property** must conservatively be modeled by *joining* v_{value} into the existing value of $v_{property}$ at v_{obj} (i.e. a *weak update*)

- This is bad for precision!

- *Strong update* (overwriting instead of joining) is possible whenever the abstract object is known to represent a single concrete object

Recency abstraction

- For each allocation site ℓ
  maintain **two** abstract objects:
  - ℓ @ corresponds to the *most recently*
      allocated object originating from ℓ
  - ℓ * older objects from ℓ
- ℓ @ always describes at most one concrete
  object and hence permits strong updating!
- To make this work, we just need some extra
  bookkeeping in the transfer functions

Interprocedural analysis with *maybe-modified*

At function exits, **restore unmodified parts of the heap (and the stack)** from the call node

Observing redundancy

```
...
TaskControlBlock.prototype.markAsRunnable = function () {
  this.state = this.state | STATE_RUNNABLE;
};
...
```

- Why is this function (from `richards.js`, V8) visited **18** times by the analyzer???

- Mostly, new dataflow that arrives at the function entry (and triggers re-analysis) is irrelevant to the function body!

Lazy propagation

- Defer propagation of field values that are not known to be relevant to the current function

- Use a placeholder value: *unknown*

- When analyzing a function, assume initially that no fields are referenced

- When a field is referenced, recover its proper value

$\Rightarrow$ irrelevant dataflow isn't propagated

$\Rightarrow$ *unknown* implies *unmodified*

An example

- Each •
  represents an
  abstract state

- For simplicity,
  no context
  sensitivity here

Formalization of lazy propagation

*How do we express the idea
more concisely and formally?*

(necessary for reasoning about its properties
and for obtaining a good implementation)

1) Start with a basic analysis framework where
   transfer functions are expressed via an
   abstract data type (ADT)

2) Introduce lazy propagation by a systematic
   modification of the ADT **(without touching
   the transfer functions!)**

The basic lattice (simplified)

object labels (allocation sites)   functions

$$\text{Value} = \mathcal{P}(L) \times \mathcal{P}(F) \times \text{Base}$$

$$\text{Obj} = P \rightarrow \text{Value}$$

property names (fields)

$$\text{State} = L \rightarrow \text{Obj}$$

$$\text{CallGraph} = \mathcal{P}(C \times N \times C \times F)$$

set of call edges

$$\text{AnalysisLattice} = (C \times N \rightarrow \text{State}) \times \text{CallGraph}$$

contexts   nodes (primitive statements)

AnalysisLattice **as an abstract data type (ADT)**

reads a field value

$$getfield : C \times N \times L \times P \rightarrow \mathsf{Value}$$

$$getcallgraph : () \rightarrow \mathsf{CallGraph}$$ reads the call graph

reads an abstract state

$$getstate : C \times N \rightarrow \mathsf{State}$$

$$propagate : C \times N \times \mathsf{State} \rightarrow ()$$ intra-procedural flow

$$funentry : C \times N \times C \times F \times \mathsf{State} \rightarrow ()$$

$$funexit : C \times N \times C \times F \times \mathsf{State} \rightarrow ()$$

inter-procedural flow

- The transfer functions can only access the AnalysisLattice element through these operations
- (We'll skip their definitions here…)

Introducing lazy propagation

– a systematic modification of the lattice and the ADT operations

property values can now be "unknown"!

$$Obj = P \to (Value\downarrow_{unknown})$$

$$CallGraph = C \times N \times C \times F \to (State\downarrow_{none})$$

$$AnalysisLattice = (C \times N \to (State\downarrow_{none})) \times CallGraph$$

now distinguishing between the *unreachable* state and the all-*unknown* state

each call edge is now labelled with an abstract state

$$recover : C \times N \times L \times P \to Value$$

used for recovering "unknown" values

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getfield' (read a field)

$a.\mathit{getfield'}(c \in C,\, n \in N,\, \ell \in L,\, p \in P):$

$\vdots$

    $v := a.\mathit{getfield}(c, n, \ell, p)$ ←   *getfield* from the basic framework

    if $v =$ unknown **then**

        // the field value has been reduced to unknown*, so recover the real value*

        $v := a.\mathit{recover}(c, n, \ell, p)$

    end if   ←   call *recover* if the value is "unknown"

    return v

$\vdots$

funentry' (flow at function entry)

$a.funentry'(c_1 \in C,\ n_1 \in N,\ c_2 \in C,\ f_2 \in F,\ s \in \textsf{State})$:
  let $(m, g) = a$ **and** $u = m(c_2, entry(f_2))$

    $\vdots$

  // *introduce* unknown *field values*
  $s' := \bot_{\textsf{State}}$
  if $u \neq$ none **then**
    for all $\ell \in L, p \in P$ **do**
      if $u(\ell)(p) \neq$ unknown **then**
        // *the field has been referenced*
        $s'(\ell)(p) := s(\ell)(p)$
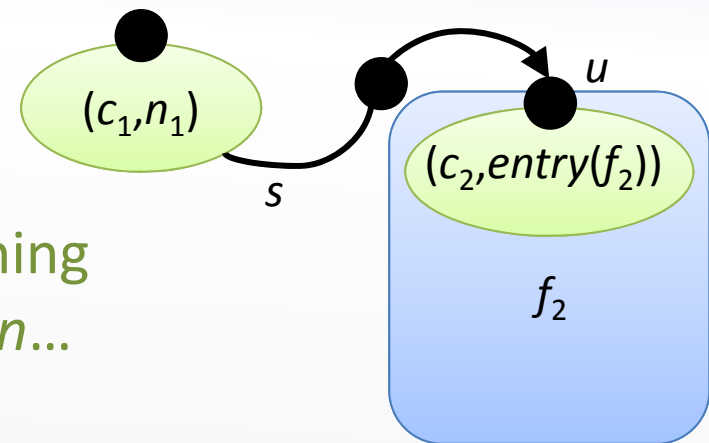   **end if**
    end for
  end if
  // *propagate the resulting state into the function entry*
  $a.propagate'(c_2, entry(f_2), s')$
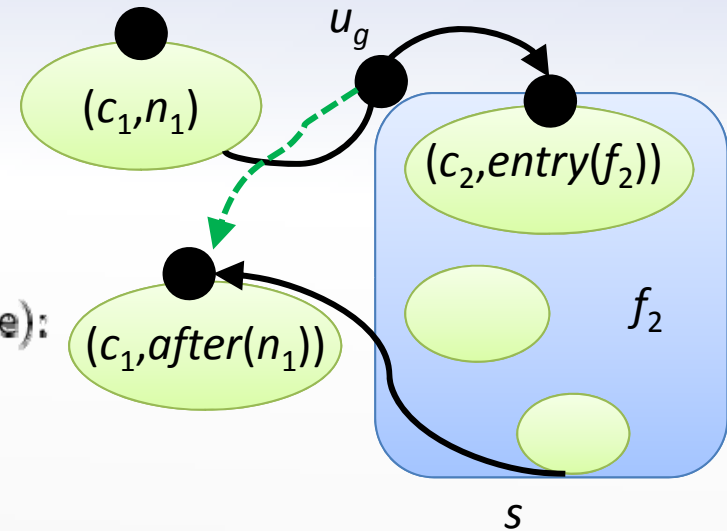
    $\vdots$

set everything
to *unknown…*

… except fields that are
known to be referenced

join *s'* into the function entry state

(c_1, n_1)

s

$(c_2, entry(f_2))$

u

f_2

funexit' (flow at function exit)

$a.funexit'(c_1 \in C, n_1 \in N, c_2 \in C, f_2 \in F, s \in \mathbf{State})$:
  let $(\_, g) = a$ **and** $u_g = g(c_1, n_1, c_2, f_2)$
  $s' := \bot_{\mathbf{State}}$
  for all $\ell \in L, p \in P$ **do**
    if $s(\ell)(p) = $ unknown **then**
      // the field has not been accessed, so restore its value from the call edge state
      $s'(\ell)(p) := u_g(\ell)(p)$
    else
      $s'(\ell)(p) := s(\ell)(p)$
    end if
  end for
  $a.propagate'(c_1, after(n_1), s')$

unknown
implies
not modified within the function

join *s'* into the node after the call

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Theoretical properties of lazy prop.

- **Precision** is at least as good as before

- **Soundness** (wrt. language semantics)
  is preserved

- **Recovery** does not affect amortized complexity

- **Number of fixpoint iterations** increases in some situations and decreases in other

Experiments

- >200 **small test cases**, to get into the obscure corner cases of JavaScript

- A few larger benchmarks: **Google's V8 benchmark suite** (500-1800 lines of code)

- Also tested on the **SunSpider benchmarks**

Experiments

Some results for `richards.js` from V8:

- the analysis guarantees for **95%** of the call/construct instructions that they always succeed

- **1** location where an absent variable is read, with **0** spurious warnings

- **93%** of all read/write/delete-property operations will never attempt to coerce null or undefined into an object

- **6** functions dead (guaranteed unreachable)

Experimental results

	LOC	Blocks	Iterations			Time (seconds)			Memory (MB)		
			lazy	*basic+*	*basic*	*lazy*	*basic+*	*basic*	*lazy*	*basic+*	*basic*
richards.js	529	478	1399	2782	2663	3.8	4.6	5.6	3.7	6.4	11.05
benchpress.js	463	710	5097	12581	18060	5.4	13.4	33.2	7.8	24.0	42.02
delta-blue.js	853	1054	63611	∞	∞	136.7	∞	∞	140.5	∞	∞
cryptobench.js	1736	2857	17213	43848	∞	22.1	99.4	∞	42.8	127.9	∞
3d-cube.js	342	545	2009	4147	7116	4.0	5.3	14.1	6.2	10.6	18.4
3d-raytrace.js	446	575	6749	30323	∞	8.2	24.8	∞	10.1	16.7	∞
crypto-md5.js	296	392	646	1004	5358	1.8	2.0	4.5	2.7	3.6	6.1
access-nbody.js	179	149	317	523	551	1.0	1.3	1.8	0.9	1.7	3.2

∞ means >512MB

basic: naive monotone framework

basic+: basic extended with *maybe-modified* (and *copy-on-write*)

lazy: basic extended with *lazy propagation*

Summary

★ ***Static analysis*** is a useful tool for reasoning about programs written in a scripting language such as JavaScript

★ ***Lazy propagation*** ensures that only relevant information is propagated from one function to another

    – reduces the amount of data being propagated

    – may improve precision: non-referenced fields respect interprocedurally realizable paths