# **Static Program Analysis** Part 10 – pointer analysis

https://cs.au.dk/~amoeller/spa/

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#### Agenda

- Introduction to pointer analysis
- Andersen's analysis
- Steensgaard's analysis
- Interprocedural pointer analysis
- Records and objects
- Null pointer analysis
- Flow-sensitive pointer analysis

# Analyzing programs with pointers

How do we perform e.g. constant propagation analysis when the programming language has pointers? (or object references?)

 $Exp \rightarrow \dots$  | alloc E | &ld | \*Exp | null

$$Stm \rightarrow \dots$$

$$| *Id = Exp;$$

# **Heap pointers**

- For simplicity, we initially ignore records
  - alloc then only allocates a single cell
  - only linear structures can be built in the heap



- Let's also ignore functions as values for now
- We still have many interesting analysis challenges...

### **Pointer targets**

- The fundamental question about pointers: What cells can they point to?
- We need a suitable abstraction
- The set of (abstract) cells, Cells, contains
  - alloc-i for each allocation site with index i
  - X for each program variable named X
- This is called *allocation site abstraction*
- Each abstract cell may correspond to many concrete memory cells at runtime

# **Points-to analysis**

- Determine for each pointer variable X the set pt(X) of the cells X may point to
- A conservative ("may points-to") analysis: <sup>\*y = -8</sup> z = \*x;
  - the set may be too large
  - can show absence of aliasing:  $pt(X) \cap pt(Y) = \emptyset$
- We'll focus on *flow-insensitive* analyses:
  - take place on the AST
  - before or together with the control-flow analysis

\*x = 42:

\*y = -87;

// is z 42 or -87?

# **Obtaining points-to information**

- An almost-trivial analysis (called *address-taken*):
  - include all alloc-i cells
  - include the X cell if the expression &X occurs in the program
- Improvement for a typed language:
  - eliminate those cells whose types do not match
- This is sometimes good enough
  - and clearly very fast to compute

# **Pointer normalization**

- Assume that all pointer usage is normalized:
  - *X* = alloc *P* where *P* is null or an integer constant
  - X = & Y
  - X = Y
  - X = \*Y
  - \*X = Y
  - *X* = null
- Simply introduce lots of temporary variables...
- All sub-expressions are now named
- We choose to ignore the fact that the cells created at variable declarations are uninitialized (otherwise it is impossible to get useful results from a flow-insensitive analysis)

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# Andersen's analysis (1/2)

- For every cell *c*, introduce a constraint variable [[*c*]] ranging over sets of cells, i.e. [[·]]: Cells → P(Cells)
- Generate constraints:
  - X = alloc P:
  - X = & Y:
  - X = Y:
  - X = \*Y:
  - \*X = Y:
  - *X* = null:

alloc $-i \in \llbracket X \rrbracket$   $Y \in \llbracket X \rrbracket$   $\llbracket Y \rrbracket \subseteq \llbracket X \rrbracket$   $c \in \llbracket Y \rrbracket \Rightarrow \llbracket c \rrbracket \subseteq \llbracket X \rrbracket$  for each  $c \in Cells$   $c \in \llbracket X \rrbracket \Rightarrow \llbracket Y \rrbracket \subseteq \llbracket c \rrbracket$  for each  $c \in Cells$ (no constraints)

(For the conditional constraints, there's no need to add a constraint for the cell x if &x does not occur in the program)

# Andersen's analysis (2/2)

- The points-to map is defined as:
   pt(X) = [X]
- The constraints fit into the cubic framework <sup>(C)</sup>
- Unique minimal solution in time  $O(n^3)$
- In practice, for Java:  $O(n^2)$
- The analysis is flow-insensitive but *directional* 
  - models the direction of the flow of values in assignments

#### **Example program**

*Cells* = {p, q, x, y, z, alloc-1}

# **Applying Andersen**

Generated constraints:

```
alloc-1 \in [[p]]

[[y]] \subseteq [[x]]

[[z]] \subseteq [[x]]

c \in [[p]] \Rightarrow [[z]] \subseteq [[c]] for each c\in Cells

[[q]] \subseteq [[p]]

y \in [[q]]

c \in [[p]] \Rightarrow [[c]] \subseteq [[x]] for each c\in Cells

z \in [[p]]
```

• Smallest solution:

```
pt(p) = { alloc-1, y, z }
pt(q) = { y }
pt(x) = pt(y) = pt(z) = Ø
```

# A specialized cubic solver

- At each load/store instruction, instead of generating a conditional constraint for each cell, generate a single universally quantified constraint:
  - $t \in \llbracket x \rrbracket$
  - $\llbracket x \rrbracket \subseteq \llbracket y \rrbracket$
  - $\forall t \in \llbracket x \rrbracket \colon \llbracket t \rrbracket \subseteq \llbracket y \rrbracket$
  - $\forall t \in \llbracket x \rrbracket \colon \llbracket y \rrbracket \subseteq \llbracket t \rrbracket$
- Whenever a token is added to a set, lazily add new edges according to the universally quantified constraints
- Note that every token is also a constraint variable here
- Still cubic complexity, but faster in practice

# A specialized cubic solver

- $x.sol \subseteq T$ : the set of tokens for x (the bitvectors)
- $x.succ \subseteq V$ : the successors of x (the edges)
- x.from  $\subseteq$  V: the first kind of quantified constraints for x
- $x.to \subseteq V$ : the second kind of quantified constraints for x
- $W \subseteq T \times V$ : a worklist (initially empty)

#### Implementation: SpecialCubicSolver

# A specialized cubic solver

- *t* ∈ [[*x*]] addToken(t, x) propagate()
- $\llbracket X \rrbracket \subseteq \llbracket Y \rrbracket$ addEdge(x, y) propagate()
- ∀t ∈ [[x]]: [[t]] ⊆ [[y]]
   add y to x.from
   for each t in x.sol
   addEdge(t, y)
   propagate()
- $\forall t \in \llbracket x \rrbracket \colon \llbracket y \rrbracket \subseteq \llbracket t \rrbracket$

add y to x.to
for each t in x.sol
 addEdge(y, t)
propagate()

addToken(t, x): if t∉x.sol add t to x.sol add (t, x) to W

addEdge(x, y): if x ≠ y ∧ y ∉ x.succ add y to x.succ for each t in x.sol addToken(t, y)

propagate(): while W ≠ Ø pick and remove (t, x) from W for each y in x.from addEdge(t, y) for each y in x.to addEdge(y, t) for each y in x.succ addToken(t, y)

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# **Steensgaard's analysis**

- View assignments as being bidirectional
- Generate constraints:
  - X = alloc P:  $alloc i \in [X]$
  - X = &Y:  $Y \in \llbracket X \rrbracket$
  - X = Y:  $\llbracket X \rrbracket = \llbracket Y \rrbracket$
  - X = \*Y:  $c \in \llbracket Y \rrbracket \Rightarrow \llbracket c \rrbracket = \llbracket X \rrbracket$  for each  $c \in Cells$
  - \*X = Y:

 $c \in \llbracket X \rrbracket \Rightarrow \llbracket Y \rrbracket = \llbracket c \rrbracket$  for each  $c \in Cells$ 

• Extra constraints:

 $c_1, c_2 \in \llbracket c \rrbracket \Rightarrow \llbracket c_1 \rrbracket = \llbracket c_2 \rrbracket$  and  $\llbracket c_1 \rrbracket \cap \llbracket c_2 \rrbracket \neq \emptyset \Rightarrow \llbracket c_1 \rrbracket = \llbracket c_2 \rrbracket$ (whenever a cell may point to two cells, they are essentially merged into one)

• Steensgaard's original formulation uses conditional unification for X = Y:  $c \in [Y] \implies [X] = [Y]$  for each  $c \in Cells$  (avoids unifying if Y is never a pointer)

# Steensgaard's analysis

- Reformulate as term unification
- Generate constraints:
  - X = alloc P: [X] = f[alloc-i]
  - X = &Y:  $\llbracket X \rrbracket = \mathbf{\uparrow} \llbracket Y \rrbracket$
  - X = Y:  $\llbracket X \rrbracket = \llbracket Y \rrbracket$
  - X = \*Y:  $[[Y]] = \mathbf{1} \alpha \land [[X]] = \alpha$  where  $\alpha$  is fresh
  - \*X = Y:

 $\llbracket X \rrbracket = \mathbf{1} \alpha \land \llbracket Y \rrbracket = \alpha$  where  $\alpha$  is fresh

- Terms:
  - term variables, e.g. [X], [alloc-i],  $\alpha$  (each representing the possible values of a cell)
  - a single (unary) term constructor  $\mathbf{1}t$  (representing pointers)
  - each [[c]] is now a term variable, not a constraint variable holding a set of cells
- Fits with our unification solver! (union-find...)
- The points-to map is defined as  $pt(X) = \{ c \in Cells \mid [X]] = \mathbf{1} [[c]] \}$
- Note that there is only one kind of term constructor, so unification never fails

# **Applying Steensgaard**

• Generated constraints (as sets or terms, respectively):

$alloc-1 \in \llbracket p \rrbracket$	[[p]] = <b>1</b> [[alloc-1]]
[[y]] = [[x]]	[[y]] = [[x]]
[[z]] = [[x]]	[[z]] = [[x]]
$c \in [\![p]\!] \Longrightarrow [\![z]\!] = [\![c]\!] \text{ for each } c \in \textit{Cells}$	$\llbracket p \rrbracket = 1 \alpha_1 \qquad \llbracket z \rrbracket = \alpha_1$
[[q]] = [[p]]	[[q]] = [[p]]
$y \in \llbracket q \rrbracket$	[[q]] = <b>1</b> [[y]]
$c \in [\![p]\!] \Longrightarrow [\![c]\!] = [\![x]\!] \text{ for each } c \in Cells$	$\llbracket p \rrbracket = 1 \alpha_2 \qquad \llbracket x \rrbracket = \alpha_2$
$z \in \llbracket p \rrbracket$	[[p]] = <b>1</b> [[z]]
+ the extra constraints	

• Smallest solution:

pt(p) = { alloc-1, y, z }
pt(q) = { alloc-1, y, z }

#### **Another example**

Andersen:



a1 = &b1; b1 = &c1; c1 = &d1; a2 = &b2; b2 = &c2; c2 = &d2; b1 = &c2;

Steensgaard:



# **Recall our type analysis...**

- Focusing on pointers...
- **Constraints:** 
  - $[X] = \mathbf{1}[P]$ • X = alloc P:
  - $[X] = \mathbf{1}[Y]$ • X = &Y:
  - $\llbracket X \rrbracket = \llbracket Y \rrbracket$ • X = Y:
  - $\mathbf{1} [\![X]\!] = [\![Y]\!]$ • X = \*Y:  $[X] = \mathbf{1}[Y]$
  - \*X = Y:
- Implicit extra constraint for term equality:  $\mathbf{1}t_1 = \mathbf{1}t_2 \Rightarrow t_1 = t_2$
- Assuming the program type checks, is the solution for pointers the same as for Steensgaard's analysis?

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# Interprocedural pointer analysis

In TIP, function values and pointers may be mixed together:

(\*\*\*x)(1,2,3)

- In this case the CFA and the points-to analysis must happen *simultaneously*!
- The idea: Treat function values as a kind of pointers

# **Function call normalization**

• Assume that all function calls are of the form

 $X = X_0(X_1, ..., X_n)$ 

• Assume that all return statements are of the form

return X';

- As usual, simply introduce lots of temporary variables...
- Include all function names in *Cells*

# **CFA with Andersen**

• For the function call  $X = X_0(X_1, ..., X_n)$ and every occurrence of  $f(X'_1, ..., X'_n)$  { ... return X'; } add these constraints:

 $f \in \llbracket f \rrbracket$  $f \in \llbracket X_0 \rrbracket \Rightarrow \left(\llbracket X_i \rrbracket \subseteq \llbracket X'_i \rrbracket \text{ for } i=1,...,n \land \llbracket X' \rrbracket \subseteq \llbracket X \rrbracket\right)$ 

- (Similarly for simple function calls)
- Fits directly into the cubic framework!

# **CFA with Steensgaard**

For the function call

 X = X<sub>0</sub>(X<sub>1</sub>, ..., X<sub>n</sub>)
 and every occurrence of
 f(X'<sub>1</sub>, ..., X'<sub>n</sub>) { ... return X'; }
 add these constraints:

 $f \in \llbracket f \rrbracket$  $f \in \llbracket X_0 \rrbracket \Rightarrow (\llbracket X_i \rrbracket = \llbracket X'_i \rrbracket \text{ for } i=1,...,n \land \llbracket X' \rrbracket = \llbracket X \rrbracket)$ 

- (Similarly for simple function calls)
- Fits into the unification framework, but requires a generalization of the ordinary union-find solver

```
foo(a) {
  return *a;
}
bar() {
  x = alloc null; // alloc-1
  y = alloc null; // alloc-2
  *x = alloc null; // alloc-3
  *y = alloc null; // alloc-4
  q = foo(x);
 w = foo(y);
}
```

Are q and w aliases?

- Generalize the abstract domain Cells → P(Cells) to Contexts → Cells → P(Cells)
   (or equivalently: Cells × Contexts → P(Cells))
   where Contexts is a (finite) set of call contexts
- As usual, many possible choices of *Contexts* recall the call string approach and the functional approach
- We can also track the set of reachable contexts (like the use of lifted lattices earlier):

 $Contexts \rightarrow lift(Cells \rightarrow \mathcal{P}(Cells))$ 

• Does this still fit into the cubic solver?



Are x and y aliases?

[[X]] = {alloc-1} [[Y]] = {alloc-1}

- We can go one step further and introduce context-sensitive heap (a.k.a. heap cloning)
- Let each abstract cell be a pair of
  - alloc-i (the alloc with index i) or X (a program variable)
  - a heap context from a (finite) set *HeapContexts*
- This allows abstract cells to be named by the source code allocation site and (information from) the current context
- One choice:
  - set HeapContexts = Contexts
  - at alloc, use the entire current call context as heap context

# Context-sensitive pointer analysis with heap cloning

Assuming we use the call string approach with k=1, so *Contexts* = { $\epsilon$ , c1, c2}, and *HeapContexts* = *Contexts* 

```
mk() {
  return alloc null; // alloc-1
}
baz() {
  var x,y;
  x = mk(); // c1
  y = mk(); // c2
 ....
}
```

Are x and y aliases?

 $[[X]] = \{ (alloc-1, c1) \}$  $[[Y]] = \{ (alloc-1, c2) \}$ 

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#### **Records in TIP**

- Field write operations: see SPA...
- Values of record fields cannot themselves be records
- After normalization:
  - $X = \{ F_1 : X_1, ..., F_k : X_k \}$
  - $X = alloc \{ F_1 : X_1, ..., F_k : X_k \}$
  - X = Y.F

Let us extend Andersen's analysis accordingly...

# **Constraint variables for record fields**

- [[·]]: (Cells ∪ (Cells × Fields)) → P(Cells) where Fields is the set of field names in the program
- Notation: [[c . f]] means [[(c, f)]]

# **Analysis constraints**

- $X = \{ F_1 : X_1, \dots, F_k : X_k \}$ :  $[X_1] \subseteq [X.F_1] \land \dots \land [X_k] \subseteq [X.F_k]$
- $X = \text{alloc} \{ F_1 \colon X_1, \dots, F_k \colon X_k \}$ :  $\text{alloc} -i \in \llbracket X \rrbracket \land$  $\llbracket X_1 \rrbracket \subseteq \llbracket \text{alloc} -i.F_1 \rrbracket \land \dots \land \llbracket X_k \rrbracket \subseteq \llbracket \text{alloc} -i.F_k \rrbracket$
- X = Y.F:  $\llbracket Y.F \rrbracket \subseteq \llbracket X \rrbracket$
- X = Y:  $\llbracket Y \rrbracket \subseteq \llbracket X \rrbracket \land \llbracket Y.F \rrbracket \subseteq \llbracket X.F \rrbracket$  for each  $F \in Fields$
- X = \*Y:  $c \in [Y] \Rightarrow ([c] \subseteq [X] \land [c.F] \subseteq [X.F])$ for each  $c \in Cells$  and  $F \in Fields$
- \*X = Y:  $c \in [X] \implies ([Y] \subseteq [c] \land [Y.F] \subseteq [c.F])$ for each  $c \in Cells$  and  $F \in Fields$

See example in SPA

#### **Objects as mutable heap records**

- E.X in Java corresponds to (\*E).X in TIP (or C)
- Can only create pointers to heap-allocated records (=objects), not to variables or to cells containing non-record values

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# Null pointer analysis

- Decide for every dereference \*p, is p different from null?
- (Why not just treat null as a special cell in an Andersen or Steensgaard-style analysis?)
- Use the monotone framework

   assuming that a points-to map *pt* has been computed
- Let us consider an intraprocedural analysis (i.e. we ignore function calls)

# A lattice for null analysis

• Define the simple lattice *Null*:



where NN represents "definitely **n**ot **n**ull" and ? represents "maybe null"

• Use for every program point the map lattice: Cells  $\rightarrow$  Null

(here for TIP without records)

# Setting up

- For every CFG node, v, we have a variable [[v]]:
  - a map giving abstract values for all cells at the program point *after* v
- Auxiliary definition:

 $JOIN(v) = \bigsqcup_{w \in pred(v)} \llbracket w \rrbracket$ 

(i.e. we make a *forward* analysis)



- For operations involving pointers:
  - X = alloc P: [v] = ???
  - X = &Y: [v] = ???
  - X = Y: [v] = ???
  - X = \*Y: [v] = ???
  - \*X = Y: [v] = ???
  - X = null: [[v]] = ???

where *P* is null or an integer constant

- For all other CFG nodes:
  - [[v]] = *JOIN*(v)

- For a heap store operation \*X = Y we need to model the change of whatever X points to
- That may be *multiple* abstract cells
   (i.e. the cells *pt(X)*)
- With the present abstraction, each abstract heap cell alloc-*i* may describe *multiple* concrete cells
- So we settle for **weak** update:

X = Y: [v] = store(JOIN(v), X, Y)

where *store*( $\sigma$ , X, Y) =  $\sigma[\alpha \mapsto \sigma(\alpha) \sqcup \sigma(Y)]$  $\alpha \in pt(X)$ 

- For a heap load operation X = \*Y we need to model the change of the program variable X
- Our abstraction has a *single* abstract cell for *X*
- That abstract cell represents a *single* concrete cell
- So we can use **strong** update:

$$X = *Y: \qquad [[v]] = load(JOIN(v), X, Y)$$
  
where 
$$load(\sigma, X, Y) = \sigma[X \mapsto \bigsqcup \sigma(\alpha)]$$

# Strong and weak updates



The abstract cell alloc-1 corresponds to multiple concrete cells

#### Strong and weak updates



The points-to set for x contains *multiple abstract cells* 

 $\llbracket v \rrbracket = JOIN(v)[X \mapsto NN, a]loc-i \mapsto ?]$ 

- *X* = alloc *P*:
- X = &Y:  $\llbracket v \rrbracket = JOIN(v)[X \mapsto NN]$
- X = Y:  $\llbracket v \rrbracket = JOIN(v)[X \mapsto JOIN(v)(Y)]$
- *X* = null:

 $\llbracket v \rrbracket = JOIN(v)[X \mapsto ?]$ 

could be improved...

- In each case, the assignment modifies a program variable
- So we can use strong updates, as for heap load operations

# Strong and weak updates, revisited

- Strong update:  $\sigma[c \mapsto new-value]$ 
  - possible if c is known to refer to a single concrete cell
  - works for assignments to local variables (as long as TIP doesn't have e.g. nested functions)
- Weak update:  $\sigma[c \mapsto \sigma(c) \sqcup new-value]$ 
  - necessary if c may refer to multiple concrete cells
  - bad for precision, we lose some of the power of flow-sensitivity
  - required for assignments to heap cells (unless we extend the analysis abstraction!)

# Interprocedural null analysis

- Context insensitive or context sensitive, as usual...
  - at the after-call node, use the heap from the callee
- But be careful! *Pointers to local variables may escape to the callee* 
  - the abstract state at the after-call node cannot simply copy the abstract values for local variables from the abstract state at the call node



# Using the null analysis

- The pointer dereference \*p is "safe" at entry of v if JOIN(v)(p) = NN
- The quality of the null analysis depends on the quality of the underlying points-to analysis

### **Example program**

```
p = alloc null;
q = &p;
n = null;
*q = n;
*p = n;
```

Andersen generates:

```
pt(p) = {alloc-1}
pt(q) = {p}
pt(n) = Ø
```

#### **Generated constraints**

```
 \begin{array}{l} \llbracket p=a \\ \exists p=a
```

# Solution

```
\begin{split} & [[p=a]] \circ c \quad null] ] = [p \mapsto NN, q \mapsto NN, n \mapsto NN, all \circ c-1 \mapsto ?] \\ & [[q=&p]] = [p \mapsto NN, q \mapsto NN, n \mapsto NN, all \circ c-1 \mapsto ?] \\ & [[n=null]] = [p \mapsto NN, q \mapsto NN, n \mapsto ?, all \circ c-1 \mapsto ?] \\ & [[*q=n]] = [p \mapsto ?, q \mapsto NN, n \mapsto ?, all \circ c-1 \mapsto ?] \\ & [[*p=n]] = [p \mapsto ?, q \mapsto NN, n \mapsto ?, all \circ c-1 \mapsto ?] \end{split}
```

- At the program point before the statement \*q=n the analysis now knows that q is definitely non-null
- ... and before \*p=n, the pointer p is maybe null
- Due to the weak updates for all heap store operations, precision is bad for alloc-i cells

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# **Points-to graphs**

- Graphs that describe possible heaps:
  - nodes are abstract cells
  - edges are possible pointers between the cells
- The lattice of points-to graphs is  $\mathcal{P}(Cells \times Cells)$ ordered under subset inclusion (or alternatively,  $Cells \rightarrow \mathcal{P}(Cells)$ )
- For every CFG node, v, we introduce a constraint variable [[v]] describing the state *after* v
- Intraprocedural analysis (i.e. ignore function calls)

# Constraints

- For pointer operations:
  - X = alloc P:  $\llbracket v \rrbracket = JOIN(v) \downarrow X \cup \{ (X, alloc i) \}$
  - X = &Y:  $\llbracket v \rrbracket = JOIN(v) \downarrow X \cup \{(X, Y)\}$
  - X = Y:  $\llbracket v \rrbracket = JOIN(v) \downarrow X \cup \{ (X, t) \mid (Y, t) \in JOIN(v) \}$
  - X = \*Y:  $\llbracket v \rrbracket = JOIN(v) \downarrow X \cup \{ (X, t) \mid (Y, s) \in \sigma, (s, t) \in JOIN(v) \}$
  - \*X = Y:  $[v] = JOIN(v) \cup \{(s, t) \mid (X, s) \in JOIN(v), (Y, t) \in JOIN(v)\}$
  - $X = null: [v] = JOIN(v) \downarrow X$

where  $\sigma \downarrow X = \{ (s,t) \in \sigma \mid s \neq X \}$ 

- For all other CFG nodes:
  - [[v]] = *JOIN*(v)

$$JOIN(v) = \bigcup_{w \in pred(v)} [w]$$

note: weak update!

#### **Example program**

```
var x,y,n,p,q;
x = alloc null; y = alloc null;
*x = null; *y = y;
n = input;
while (n>0) {
  p = alloc null; q = alloc null;
  *p = x; *q = y;
 x = p; y = q;
 n = n - 1;
}
```

# **Result of analysis**

• After the loop we have this points-to graph:



• We conclude that x and y will always be disjoint

# Points-to maps from points-to graphs

A points-to map for each program point v:
 pt(X) = { t | (X,t) ∈ [[v]] }

- More expensive, but more precise:
  - Andersen:  $pt(x) = \{y, z\}$
  - flow-sensitive: pt(x) = { z }

			-	
X	( =	=	&z	
X				

# Improving precision with abstract counting

- The points-to graph is missing information: - alloc-2 nodes always form a self-loop in the example
- We need a more detailed lattice:  $\mathcal{P}(Cells \times Cells) \times (Cell \rightarrow Count)$ where we for each cell keep track of how many concrete cells that abstract cell describes Count = 0
- This permits strong updates on those that describe precisely 1 concrete cell

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>1

#### **Better results**

• After the loop we have this extended points-to graph:



- Thus, alloc-2 cells form a self-loop
- Both alloc-1 and alloc-2 permit strong updates

# **Escape analysis**

- Perform a points-to analysis
- Look at return expression
- Check reachability in the points-to graph to arguments or variables defined in the function itself
- None of those
   U
   no escaping stack cells

```
baz() {
  var x;
  return &x;
}
main() {
  var p;
  p=baz();
  *p=1;
  return *p;
}
```